

# THERMODYNAMIC PROPERTIES OF THE BINARY MIXTURE OF WATER AND *n*-BUTANOL

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The molar heat capacities of the binary mixture composed of water and *n*-butanol were measured with an adiabatic calorimeter in the temperature range 78–320 K. The functions of the heat capacity with respect to thermodynamic temperature were established. A glass transition, solid–solid phase transition and solid–liquid phase transition were observed. The corresponding enthalpy and entropy of the solid–liquid phase transition were calculated, respectively. The thermodynamic functions relative to a temperature of 298.15 K were derived based on the relationships of the thermodynamic functions and the function of the measured heat capacity with respect to temperature.

**Keywords:** adiabatic calorimetry, heat capacity, low temperature, *n*-butanol, water

## Introduction

In previous reports, the heat capacities of azeotropic systems composed of water+ethanol and water+*n*-propanol have been investigated [1, 2]. Heat capacity is one of the more valuable thermophysical quantities to be considered when studying pure liquids and liquid mixtures. Accurate values are needed in many areas of physics, chemistry, and chemical engineering for establishing energy balances, obtaining entropy and enthalpy values, or studying phase transitions. Moreover, ascertainment of the heat capacity of liquids as a function of temperature is a source of important information concerning their molecular structure and is essential for checking the efficiency of estimation models used in industry [3]. The adiabatic calorimeter is the most important and accurate tool for heat capacity determination over a wide range of temperatures. An adiabatic calorimeter has been described and used to measure heat capacities of samples in our previous research [4–9]. Moving along these lines, the heat capacity of the binary mixture composed of water and *n*-butanol was studied.

In a series of alkane-mono-ols in increasing order of the number of carbon atoms, *n*-butanol (abbreviated as 1B hereinafter) is the first that exhibits a limited solubility in water [10]. At about  $x_{1B}=0.018$  and 298.15 K phase separation occurs, where  $x_{1B}$  is the mole fraction of 1B. The equilibrium composition of the 1B-rich phase is  $x_{1B}=0.49$ . Thermodynamic properties have been investigated for the systems composed of 1B and H<sub>2</sub>O at 298.15 K [11, 12].

In this study, the molar heat capacity of the binary mixture composed of 1B and H<sub>2</sub>O was measured by an adiabatic calorimeter in temperature range of 78–320 K. The thermodynamic functions of the binary mixture were derived based on the relationships of the thermodynamic functions and the function of the measured heat capacity with respect to temperature.

## Experimental

The *n*-butanol used for calorimetric study was purchased from Shenyang Chemical Agent Factory, and its purity was better than 99.8 mass%. The principal impurities were carbonyl compound and unsaturated compound, which contents were all smaller than 0.02%. The water used for preparing the binary mixture was deionized and distilled twice. The investigated system is composed of  $x_{1B}=0.0263$ , 0.311 and 0.686, respectively.

The mass of the binary mixture used for heat-capacity measurements was 29.6802, 29.8419 and 29.7322 g for the systems composed of  $x_{1B}=0.0263$ , 0.311 and 0.686, respectively.

Heat capacity measurements were carried out in a high-precision automatic adiabatic calorimeter described in detail elsewhere [2, 4]. The principle of the calorimeter is based on the Nernst stepwise heating method. All the data were automatically picked up through a Data Acquisition/Switch Unit (Model: 34970A, Agilent, USA) and processed by a computer.

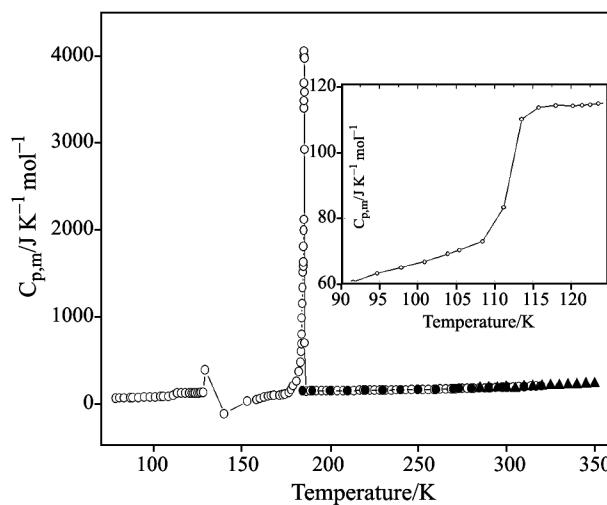
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To verify the reliability of the adiabatic calorimeter, the molar heat capacities for the reference standard material  $\alpha\text{-Al}_2\text{O}_3$ , water and 1B were measured. The deviations of our experimental results from the values were within  $\pm 0.2\%$  in a temperature range of (80 to 400) K for  $\alpha\text{-Al}_2\text{O}_3$  [13]. The molar heat capacities of water were given in reference [2]. Plots of molar heat capacities of 1B as a function of temperature are given in Fig. 1. In order to compare the results of the molar heat capacities of 1B measured in our laboratory with references [14, 15], the data of heat capacities gained from the references are given in Fig. 1 as well. The enthalpy  $\Delta_{\text{trs}}H_m$  and entropy  $\Delta_{\text{trs}}S_m$  of the phase transition were calculated according to the relationship given by,

$$\Delta_{\text{trs}}H_m = \frac{Q - n \int_{T_1}^{T_{\text{trs}}} C_{p,m(S)} dT - n \int_{T_{\text{trs}}}^{T_2} C_{p,m(L)} dT - n \int_{T_1}^{T_2} C_0 dT}{n} \quad (1)$$

and

$$\Delta_{\text{trs}}S_m = \frac{\Delta_{\text{trs}}H_m}{T_{\text{trs}}} \quad (2)$$



**Fig. 1** Molar heat capacities of *n*-butanol: ○ – this work, ▲ – [15], ● – [14]. Inset 1 shows the glass-transition of *n*-butanol

where  $Q$  is the total amount of heat introduced into the sample cell;  $n$  the amount of substance of the sample;  $T_{\text{trs}}$  phase transition temperature,  $T_1$  slightly below  $T_{\text{trs}}$ ;  $T_2$  slightly above  $T_{\text{trs}}$ ;  $C_{p,m(S)}$ ,  $C_{p,m(L)}$ ,  $C_0$  the heat capacity in solid and liquid state and heat capacity of empty cell, respectively. The phase transition temperatures, enthalpies and entropies for 1B are given in Table 1.

Figure 1 and Table 1 show that the molar heat capacities, the phase transition temperature and enthalpy determined in our laboratory are in excellent agreement with the data cited from the references.

## Result and discussion

### Molar heat capacity of the binary mixture

The molar heat capacities of the binary mixtures composed of  $x_{1B}=0.0263$ , 0.311 and 0.686, were determined by using the adiabatic calorimeter in the temperature range of 78–320 K. The results of the molar heat capacities are listed in Table 2 and shown in Fig. 2. No thermal anomaly was observed or no phase transition took place in the temperature range 185–260 K and 275–320 K, respectively.

The values of molar heat capacities of the binary mixtures were fitted in the following polynomial expressions with least square method.

$$C_{p,m}/R = \sum_{i=0}^n a_i (T/100)^i \quad (3)$$

where  $C_{p,m}/R$  is the molar heat capacity of the mixture,  $T/K$  thermodynamic temperature,  $R=8.314 \text{ J mol}^{-1} \text{ K}^{-1}$ . The fitting results were given in Table 3.

### Thermodynamic data of glass and phase transitions

It can be seen from Figs 1 and 2a, and Table 2, that the heat capacity jump was found in the temperature range 105–115 K for the pure 1B and the binary mixtures composed of  $x_{1B}=0.311$  and 0.686, respectively. The heat capacity changes clearly before and after glass transition temperature [16]. Then, the glass tran-

**Table 1** Data of the transition temperature, enthalpy and entropy for the glass transition, solid–solid and solid–liquid phase transition

$x_{1B}$	$T_g/\text{K}$	$T_{s-s}/\text{K}$	$T_{s-l}/\text{K}$	$\Delta H_{\text{trs}}/\text{kJ mol}^{-1}$	$\Delta S_{\text{trs}}/\text{J mol}^{-1} \text{ K}^{-1}$
1	111.21	129.26	184.45	9.278	50.30
			183.9 [14]	9.282 [14]	
0.686	111.65	130.07	181.44		
			269.10	1.589	5.905
0.311	111.97	134.96	180.20		
			269.37	3.847	14.28
0.0263		179.73	179.73	0.236	1.313
			270.33	5.482	20.28

sition took place in the temperature range. The temperatures of the glass transition for the systems, at which the value of  $dC_{p,m}/dT$  reaches the maximum, were determined and listed in Table 1. It can be seen from Table 1 that the glass transition temperature  $T_g$  for the systems is increasing with  $x_{1B}$  decrease.  $T_g$  increases when the molecular structure becomes more rigid [17]. The same phenomenon was found in the binary system of water and ethanol [1]. For  $x_{1B}=0.0263$  system, the glass transition did not take place. The reason may be that, in the most water-rich region, the

hydrogen-bond of bulk is high enough to retain the hydrogen-bond connectivity throughout the entire bulk called ‘mixing scheme I’ as pure water in this mixture [11]. A glass transition took place because of 1B added in the binary mixture. With  $x_{1B}$  increasing, the structure of the bulk is changing into ‘mixing scheme II’ for the binary system.

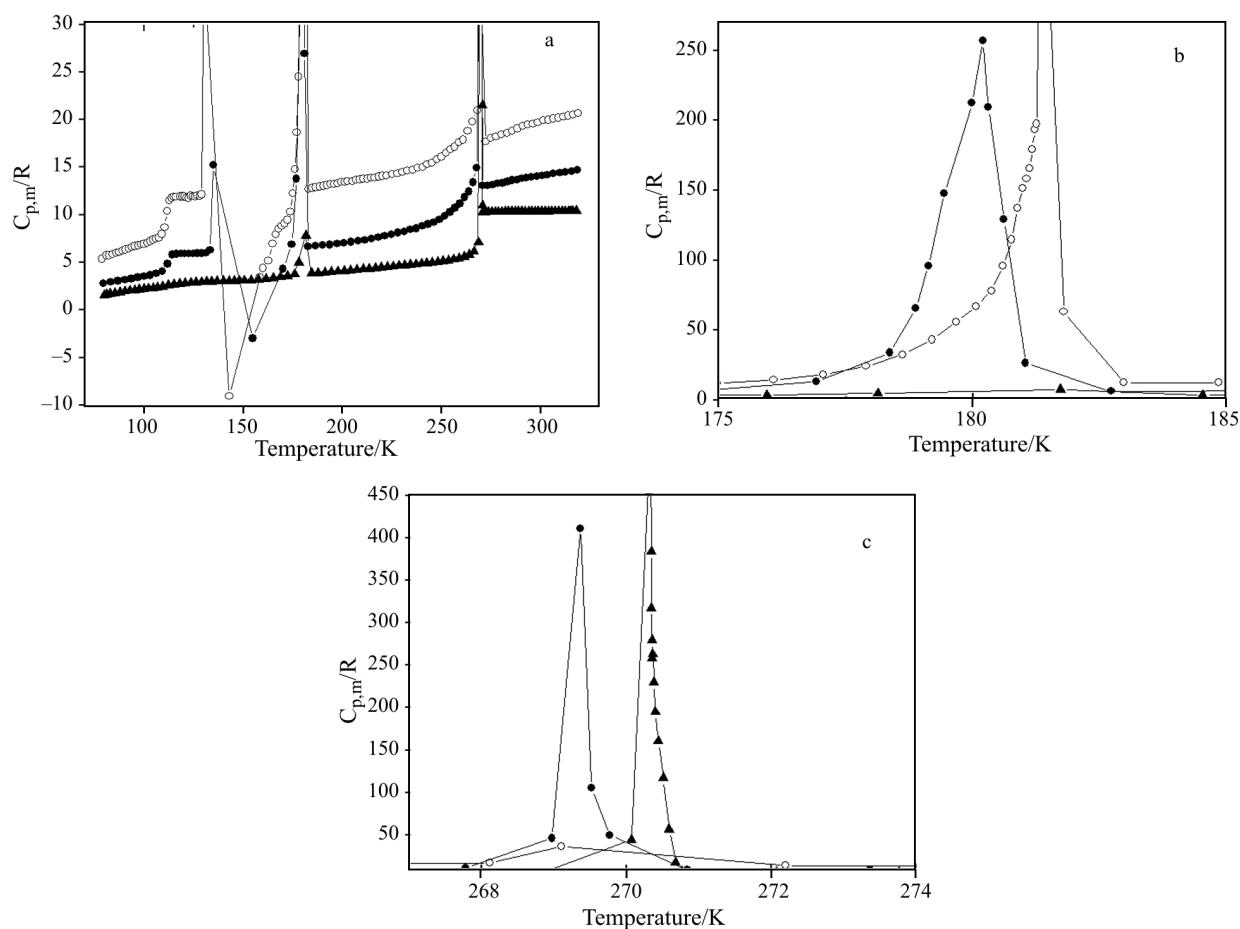
The molar heat capacity reaches maxima in temperature range of 130–150 K for  $x_{1B}=1$ , 0.686 and 0.311 systems, 178–185 K for  $x_{1B}=1$ , 0.686, 0.311 and 0.0263 systems, 266–271 K for  $x_{1B}=0.686$ , 0.311

**Table 2** Molar heat capacity of the binary mixture

$T/K$	$C_{p,m}/R$	$T/K$	$C_{p,m}/R$	$T/K$	$C_{p,m}/R$	$T/K$	$C_{p,m}/R$	$T/K$	$C_{p,m}/R$
$x_{1B}=0.686$									
78.86	5.418	120.27	11.91	180.07	67.12	195.83	13.23	256.79	17.08
81.01	5.761	121.39	11.82	180.37	78.44	197.63	13.29	258.94	17.57
82.47	5.778	122.50	11.75	180.59	96.04	199.42	13.44	261.04	17.84
84.16	5.914	123.61	11.99	180.76	114.7	201.20	13.44	263.28	18.74
85.83	6.046	124.73	11.97	180.88	137.1	202.70	13.50	265.69	19.70
87.49	6.130	125.83	11.91	180.99	151.2	205.12	13.50	268.12	20.88
89.12	6.256	126.95	12.03	181.06	158.2	206.97	13.64	269.10	40.13
90.73	6.373	128.06	11.99	181.12	165.8	208.89	13.70	272.20	17.63
92.33	6.505	129.18	12.11	181.17	179.4	210.78	13.77	274.95	17.99
93.91	6.638	130.07	36.69	181.22	193.1	212.67	13.77	277.67	18.19
95.47	6.719	143.06	-8.905	181.25	197.3	214.55	13.84	280.38	18.36
97.02	6.819	158.36	3.488	181.29	341.1	216.41	13.84	283.06	18.54
98.57	6.922	160.13	4.450	181.34	351.2	218.26	13.98	285.73	18.77
100.09	6.959	162.75	5.218	181.37	363.7	220.10	14.05	288.38	18.99
101.61	7.086	164.86	7.012	181.39	397.8	222.38	14.12	291.01	19.24
103.12	7.251	166.55	7.956	181.42	397.4	225.10	14.25	293.61	19.43
104.62	7.413	168.04	8.519	181.44	402.9	227.78	14.33	296.21	19.49
106.12	7.525	169.51	8.855	181.46	388.9	230.35	14.43	298.81	19.63
107.59	7.649	170.96	9.102	181.48	347.1	232.95	14.60	301.38	19.85
109.04	8.000	172.39	9.472	181.52	288.1	235.51	14.67	303.94	19.91
110.42	8.719	173.74	10.33	181.79	63.48	238.06	14.88	306.48	20.05
111.65	10.39	174.97	12.25	182.98	12.71	240.51	15.01	309.00	20.12
112.77	11.49	176.08	14.75	184.85	12.81	242.91	15.29	311.52	20.24
113.89	11.77	177.06	18.61	186.70	12.88	245.30	15.43	314.01	20.34
115.01	11.86	177.90	24.40	188.54	12.94	247.70	15.77	316.49	20.45
116.13	11.87	178.63	32.80	190.37	13.01	250.06	16.05	319.08	20.57
118.04	11.92	179.20	43.41	192.21	13.09	252.35	16.47		
119.16	11.91	179.68	56.20	194.02	13.23	254.60	16.84		
$x_{1B}=0.311$									
79.51	2.862	129.14	6.013	186.45	6.770	246.12	9.230	280.84	13.33
83.27	3.011	131.28	6.032	190.13	6.837	248.94	9.504	283.30	13.46
86.84	3.111	133.38	6.331	193.78	6.902	251.69	9.851	285.74	13.59
90.30	3.232	134.96	15.18	197.38	6.989	254.32	10.28	288.15	13.68
93.64	3.350	154.78	-2.875	200.96	7.080	256.87	10.72	290.53	13.80
96.88	3.475	170.21	4.373	204.49	7.173	259.33	11.17	292.88	13.84
100.05	3.595	174.53	6.949	207.98	7.293	261.67	11.84	295.42	13.93
103.15	3.712	176.92	13.76	211.44	7.390	263.87	12.44	298.15	14.01
106.21	3.879	178.36	34.11	214.84	7.516	265.90	13.38	300.82	14.11
109.20	4.133	178.88	65.77	218.21	7.659	267.78	14.91	303.44	14.19
111.97	4.889	179.13	95.81	221.52	7.817	268.98	49.57	306.52	14.29
114.26	5.831	179.44	147.8	224.78	7.977	269.37	410.3	309.87	14.38
116.50	5.945	179.98	212.2	227.99	8.142	269.52	108.4	312.48	14.46
118.70	5.952	180.20	256.6	231.16	8.279	269.77	53.06	315.62	14.56
120.50	5.962	180.30	209.2	234.29	8.450	270.85	13.06	318.74	14.66
122.68	5.967	180.61	129.2	237.34	8.588	273.36	13.06		
124.84	5.986	181.04	26.82	240.32	8.853	275.87	13.15		
127.00	5.998	182.73	6.699	243.25	9.022	278.36	13.28		

Table 2 Continued

T/K	$C_{p,m}/R$	T/K	$C_{p,m}/R$	T/K	$C_{p,m}/R$	T/K	$C_{p,m}/R$	T/K
$x_{1B}=0.0263$								
79.92	1.660	140.12	3.103	216.68	4.450	270.33	1143	283.85
81.16	1.695	142.93	3.116	219.73	4.520	270.34	659.1	285.52
82.95	1.775	145.54	3.124	222.74	4.586	270.34	534.0	287.19
85.25	1.861	148.14	3.157	225.70	4.636	270.34	488.2	288.86
87.83	1.933	150.76	3.165	228.60	4.691	270.35	383.4	290.54
90.38	2.040	153.98	3.202	231.47	4.750	270.35	317.9	292.21
92.86	2.117	157.78	3.254	234.33	4.802	270.36	280.7	293.89
95.28	2.176	161.53	3.315	237.16	4.865	270.36	259.1	295.56
97.65	2.225	165.27	3.414	239.93	4.931	270.37	263.8	297.24
99.98	2.286	168.90	3.535	242.63	4.980	270.38	231.5	298.93
102.28	2.344	172.47	3.642	245.36	5.022	270.40	197.1	300.61
104.54	2.391	175.95	3.813	248.13	5.092	270.45	162.9	302.29
106.76	2.447	178.14	5.055	250.85	5.180	270.51	120.0	303.97
109.36	2.526	179.73	7.852	253.56	5.272	270.59	59.86	305.66
112.32	2.665	184.53	3.898	256.23	5.368	270.68	21.45	307.35
115.19	2.757	187.89	3.929	258.87	5.492	270.77	10.98	309.04
118.00	2.809	191.21	4.003	261.46	5.624	270.87	10.29	310.73
120.79	2.866	194.51	4.061	264.00	5.838	272.07	10.30	312.42
123.54	2.917	197.77	4.111	266.46	6.200	273.77	10.32	314.02
126.25	2.960	200.99	4.161	268.76	7.161	275.46	10.32	315.11
128.93	3.018	204.18	4.215	270.07	47.91	277.13	10.33	316.01
131.57	3.053	207.35	4.268	270.30	464.7	278.81	10.33	316.45
134.21	3.034	210.49	4.339	270.32	620.9	280.50	10.34	318.17
136.85	3.103	213.60	4.378	270.32	942.9	282.17	10.34	



**Fig. 2** Molar heat capacities of the binary mixtures: a –  $\circ - x_{1B}=0.686$ ;  $\bullet - x_{1B}=0.311$ ;  $\blacktriangle - x_{1B}=0.0263$ . b – and c – show the solid–liquid phase transitions for *n*-butanol and water in the system, respectively

**Table 3** Fitting coefficients  $a_i$  and standard deviations  $\delta$ 

$x_{1B}$	$T/K$	$a_3$	$a_2$	$a_1$	$a_0$	$\delta$
0.0263	185–260	2.1617	-13.592	30.245	-19.26	0.018
	275–320		-0.0526	0.5101	9.319	0.001
0.311	185–260	14.342	-88.04	182.77	-121	0.079
	275–320		-2.179	16.417	-15.55	0.019
0.686	185–260	21.988	-138.66	293.97	-195.8	0.061
	275–320		-6.872	46.729	-58.61	0.041

**Table 4** The data of the thermodynamic functions of the binary mixture

$T/K$	$C_{p,m}/J\text{ mol}^{-1}\text{ K}^{-1}$	$\Delta H^*/\text{kJ mol}^{-1}$	$\Delta S^{**}/\text{J mol}^{-1}\text{ K}^{-1}$	$C_{p,m}/J\text{ mol}^{-1}\text{ K}^{-1}$	$\Delta H^*/\text{kJ mol}^{-1}$	$\Delta S^{**}/\text{J mol}^{-1}\text{ K}^{-1}$	$C_{p,m}/J\text{ mol}^{-1}\text{ K}^{-1}$	$\Delta H^*/\text{kJ mol}^{-1}$	$\Delta S^{**}/\text{J mol}^{-1}\text{ K}^{-1}$
	$x_B=0.686$			$x_B=0.311$			$x_B=0.0263$		
190	108.0	-12.91	-53.45	56.62	-10.72	-42.69	32.97	-9.748	-37.70
200	111.4	-11.81	-47.81	59.16	-10.14	-39.72	34.55	-9.410	-35.97
210	113.7	-10.69	-42.32	61.37	-9.534	-36.78	36.03	-9.057	-34.25
220	116.0	-9.539	-36.98	63.97	-8.907	-33.87	37.51	-8.689	-32.54
230	119.3	-8.364	-31.76	67.66	-8.251	-30.95	39.10	-8.306	-30.84
240	124.8	-7.146	-26.57	73.17	-7.548	-27.96	40.92	-7.907	-29.14
250	133.5	-5.858	-21.31	81.22	-6.779	-24.82	43.06	-7.487	-27.42
260	146.7	-4.461	-15.84	92.51	-5.913	-21.43	45.64	-7.044	-25.69
270	Phase transition			Phase transition			Phase transition		
280	152.6	-2.871	-9.932	110.9	-2.066	-7.148	85.92	-1.562	-5.406
290	158.9	-1.313	-4.464	114.2	-0.941	-3.199	86.10	-0.702	-2.388
300	164.0	0.303	1.012	117.1	0.216	0.723	86.27	0.160	0.534
310	168.0	1.964	6.459	119.7	1.401	4.608	86.42	1.023	3.365
320	170.9	3.659	11.84	122.0	2.610	8.445	86.57	1.888	6.111
298.15	163.2	0	0	116.6	0	0	86.24	0	0

\* $\Delta H=H_T-H_{298.15\text{ K}}$ ; \*\* $\Delta S=S_T-S_{298.15\text{ K}}$

and 0.0263 systems, respectively, as shown in Figs 1 and 2. The phase transition temperatures were determined and listed in Table 1, which were corresponding to the solid–solid and solid–liquid phase transitions for the 1B, and solid–liquid phase transition for the water, respectively. Comparing the data in Table 1, the solid–solid phase transition temperatures are increasing with  $x_{1B}$  decrease. The solid–liquid phase transition temperatures of 1B and water in the mixture are lower than those of pure 1B and water. For  $x_{1B}=0.0263$  system, the solid–solid phase transition for the 1B did not take place. This is in agreement with the discussion for the glass transition.

The unusual phenomenon is that the mixtures absorbed energy first and then released energy in temperature range 140–150 K for  $x_{1B}=1$ , 0.686 and 0.311 systems, as shown in Figs 1 and 2a. A kind of phase transition of a metastable crystal to a stable crystal exists has been found in the azeotropic mixture composed of water and ethanol [1]. The similar phenomenon may occur in these systems.

The enthalpies and entropies of the phase transition were calculated according to Eqs (1) and (2). The data are given in Table 1.

#### Thermodynamic functions of the binary systems

The thermodynamic functions of the binary systems were calculated based on the function of the molar heat capacity with respect to thermodynamic temperature and the relationships of the thermodynamic functions. The results are given in Table 4.

#### Conclusions

The molar heat capacity of the binary systems were measured 78–320 K. The glass transition temperature and the solid–solid phase transition temperature are increasing with  $x_{1B}$  decrease for the systems. The solid–liquid phase transition temperatures for 1B and water in the binary systems are lower than those of pure 1B and water.

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